

## A Simple Fuzzy Logic Approach for Induction Motors Stator Condition Monitoring

*Many researches dealt with the problem of induction motors fault detection and diagnosis. The major difficulty is the lack of an accurate model that describes a fault motor. Moreover, experienced engineers are often required to interpret measurement data that are frequently inconclusive. A fuzzy logic approach may help to diagnose induction motor faults. In fact, fuzzy logic is reminiscent of human thinking processes and natural language enabling decisions to be made based on vague information. Therefore, this paper applies fuzzy logic to induction motors fault detection and diagnosis. The motor condition is described using linguistic variables. Fuzzy subsets and the corresponding membership functions describe stator current amplitudes. A knowledge base, comprising rule and data bases, is built to support the fuzzy inference. The induction motor condition is diagnosed using a compositional rule of fuzzy inference.*

**Keywords:** Induction motor, diagnosis, fuzzy logic, stator current amplitudes.

### 1. INTRODUCTION

One of the most widely used techniques for obtaining information on the health state of induction motors is based on the processing of stator line current. Typically, in the motor fault diagnosis process, sensors are used to collect time domain current signals. The diagnostic expert then uses both time domain and frequency domain signals to study the motor condition and determines what faults are present [1-4]. However, experienced engineers are often required to interpret measurement data that are frequently inconclusive. A fuzzy logic approach may help to diagnose induction motor faults. In fact, fuzzy logic is reminiscent of human thinking processes and natural language enabling decisions to be made based on vague information.

Fuzzy logic allows items to be described as having a certain membership degree in a set. This allows a computer, which is normally constrained to 1 and 0, to delve into the continuous realm [5]. When conducting fault diagnosis, there are several situations in which an object is not obviously “good” or “bad”, but may fall into some interior range [6-8]. According to the fact that *induction motor condition interpretation is a fuzzy concept* [9], during the past few years,

---

Corresponding author : [m.benbouzid@ieec.org](mailto:m.benbouzid@ieec.org)

Laboratoire d'Ingénierie Mécanique et Electrique (LIME),  
IUT of Brest, University of Western Brittany Rue de Kergoat  
– BP 93169, 29231, Brest Cedex 3, France

researchers have proposed some fuzzy logic based diagnosis approaches [10-22]. A major difficulty is the lack of a well processing of fuzzy input data.

This paper applies fuzzy logic, to the diagnosis of induction motor stator and phase conditions, based on the amplitude features of stator currents. This method has been chosen because fuzzy logic has proven ability in mimicking human decisions [23], and the stator voltage and phase condition monitoring problem has typically been solved [24-25]. The motor condition is described using linguistic variables. Fuzzy subsets and the corresponding membership functions describe stator current amplitudes. A knowledge base, comprising rule and databases, is built to support the fuzzy inference. The induction motor condition is diagnosed using a compositional rule of fuzzy inference. The generality of the proposed methodology has been experimentally tested on a 4-kW squirrel-cage induction motor. The obtained results indicate that the fuzzy logic approach, as proposed by the authors, is capable of highly accurate diagnosis.

## 2. STATOR CURRENT MONITORING SYSTEM

A stator current signal contains potential fault information. The most suitable measurements for diagnosing the faults under consideration, in term of easy accessibility, reliability, and sensitivity, are the stator current amplitudes  $I_a$ ,  $I_b$ , and  $I_c$ . These amplitudes are monitored by the system illustrated by Fig. 1.

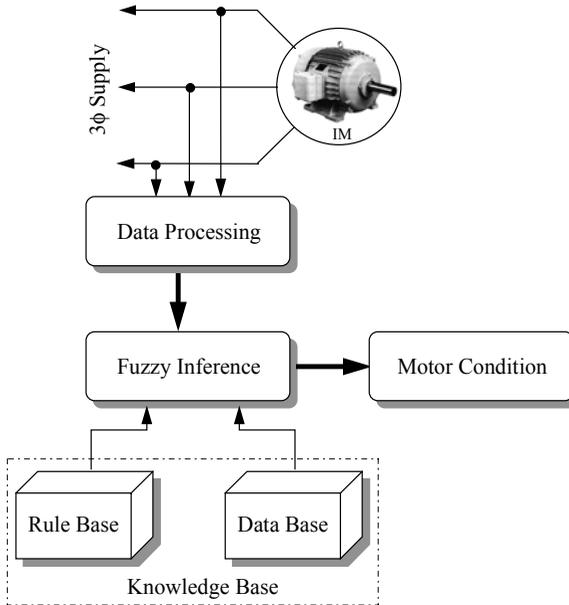


Fig. 1. Block diagram of induction motor condition monitoring system.

### 3. FUZZY LOGIC BASED DIAGNOSIS APPROACH

Fuzzy systems rely on a set of rules. These rules, while superficially similar, allow the input to be fuzzy, i.e. more like the natural way that humans express knowledge. Thus, a power engineer might refer to an electrical machine as “somewhat secure” or a “little overloaded”. This linguistic input can be expressed directly by a fuzzy system. Therefore, the natural format greatly eases the interface between the engineer knowledge and the domain expert. Furthermore, infinite graduations of truth are allowed, a characteristic that accurately mirrors the real world, where decisions are seldom “crisp” [5].

#### 3.1 Fuzzy System Input-Output Variables

As stated, the induction motor condition can be deduced by observing the stator current amplitudes. Interpretation of results is difficult as relationships between the motor condition and the current amplitudes are vague. Therefore, using fuzzy logic, numerical data are represented as linguistic information [26].

In our case, the stator current amplitudes  $I_a$ ,  $I_b$ , and  $I_c$  are considered as the input variables to the fuzzy system. The stator condition,  $CM$ , is chosen as the output variable. All the system inputs and outputs are defined using fuzzy set theory.

$$\begin{cases} I_a = \{ \mu_{I_a}(i_{aj}) / i_{aj} \in I_a \} \\ I_b = \{ \mu_{I_b}(i_{bj}) / i_{bj} \in I_b \} \\ I_c = \{ \mu_{I_c}(i_{cj}) / i_{cj} \in I_c \} \end{cases} \quad (1)$$

$$CM = \{ \mu_{CM}(cm_j) / cm_j \in CM \} \quad (2)$$

where  $i_{aj}$ ,  $i_{bj}$ ,  $i_{cj}$ , and  $cm_j$  are, respectively, the elements of the discrete universe of discourse  $I_a$ ,  $I_b$ ,  $I_c$ , and  $CM$ .  $\mu_{I_a}(i_{aj})$ ,  $\mu_{I_b}(i_{bj})$ ,  $\mu_{I_c}(i_{cj})$ , and  $\mu_{CM}(cm_j)$ , are, respectively, the corresponding membership functions.

#### 3.2 Linguistic Variables

Basic tools of fuzzy logic are linguistic variables. Their values are words or sentences in a natural or artificial language, providing a means of systematic manipulation of vague and imprecise concepts. More specifically, a linguistic variable is characterized by a quintuple  $(x, T(x), U, G, M)$ , where  $x$  is the variable name;  $T(x)$  is the set of names of the linguistic values of  $x$ , each a fuzzy variable, denoted generically by  $x$  and ranging over a universe of discourse  $U$ .  $G$  is a

syntactic rule for generating the names of  $x$  values;  $M$  is the semantic rule associating a meaning with each value.

For instance, the term set  $T(CM)$ , interpreting stator condition,  $CM$ , as a linguistic variable, could be

$$T(CM) = \{Good, Damage, Seriously Damaged\} \tag{3}$$

Where each term in  $T(CM)$  is characterized by a fuzzy subset, in a universe of discourse  $CM$ . *Good* might be interpreted as *a stator with no faults*, *damaged* as *a stator with voltage unbalance*, and *seriously damaged* as *a stator with an open phase*. Figure 2 gives an illustration of the stator condition as a linguistic variable.

Similarly, the input variables  $I_a$ ,  $I_b$ , and  $I_c$  are interpreted as linguistic variables, with

$$T(Q) = \{Zero, Small, Medium, Big\} \tag{4}$$

Where  $Q = I_a, I_b, I_c$ , respectively.

### 3.3 Fuzzy and Membership Functions Construction

Fuzzy rules and membership functions are constructed by observing the data set. For the measurements related to the stator currents, more insight into the data is needed, so membership functions will be generated for *zero*, *small*, *medium*, and *big*. For the measurement related to the stator condition, it is only necessary to know if the stator condition is *good*, *damaged*, or *seriously damaged*. The optimized membership functions for this problem are shown in Figs. 3 and 4. Once the form of the initial membership functions has been determined, the fuzzy *if-then* rules can be derived. In this study, two faults have been investigated: stator voltage unbalance and open phase.

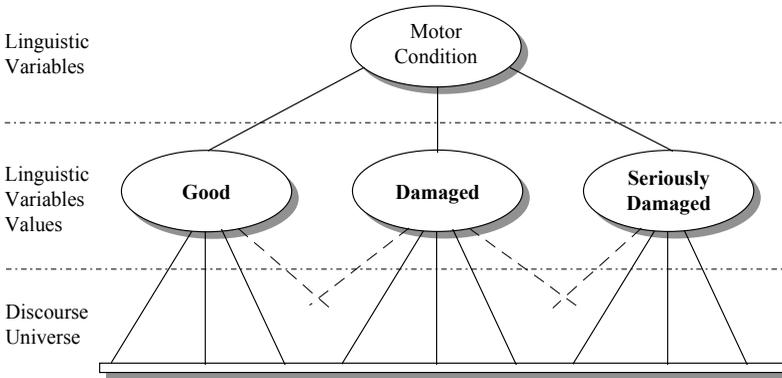


Fig. 2. Linguistic variables of the induction motor stator condition.

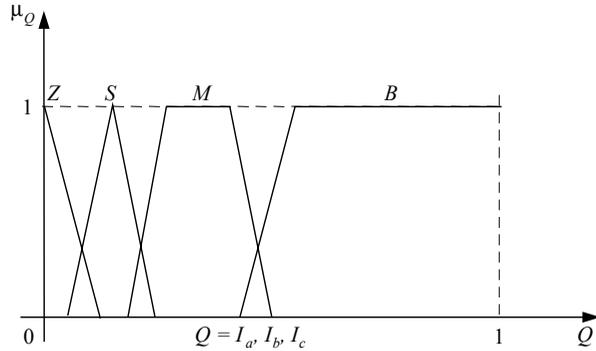


Fig. 3. Fuzzy membership functions for stator currents.  
(Z: Zero, S: Small, M: Medium, and B: Big)

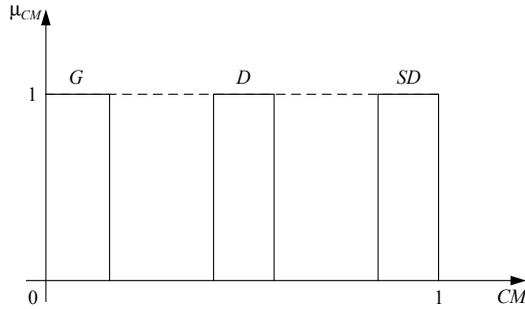


Fig. 4. Fuzzy membership functions for the stator condition.  
(G: Good, D: Damaged, and SD: Seriously Damaged)

These rules have been optimized so as to cover all the healthy and the faulty cases. For our study, we have obtained the following 14 *if-then* rules.

- Rule (1) : If  $I_a$  is Z Then CM is SD
- Rule (2) : If  $I_b$  is Z Then CM is SD
- Rule (3) : If  $I_c$  is Z Then CM is SD
- Rule (4) : If  $I_a$  is B Then CM is SD
- Rule (5) : If  $I_b$  is B Then CM is SD
- Rule (6) : If  $I_c$  is B Then CM is SD
- Rule (7) : If  $I_a$  is S and  $I_b$  is S and  $I_c$  is M Then CM is D
- Rule (8) : If  $I_a$  is S and  $I_b$  is M and  $I_c$  is M Then CM is D
- Rule (9) : If  $I_a$  is M and  $I_b$  is S and  $I_c$  is M Then CM is D

- Rule (10) : If  $I_a$  is  $M$  and  $I_b$  is  $M$  and  $I_c$  is  $M$  Then  $CM$  is  $G$
- Rule (11) : If  $I_a$  is  $S$  and  $I_b$  is  $S$  and  $I_c$  is  $S$  Then  $CM$  is  $G$
- Rule (12) : If  $I_a$  is  $S$  and  $I_b$  is  $M$  and  $I_c$  is  $S$  Then  $CM$  is  $D$
- Rule (13) : If  $I_a$  is  $M$  and  $I_b$  is  $S$  and  $I_c$  is  $S$  Then  $CM$  is  $D$
- Rule (14) : If  $I_a$  is  $M$  and  $I_b$  is  $M$  and  $I_c$  is  $S$  Then  $CM$  is  $D$

#### **4. EXPERIMENTAL PROCESS**

Figures 5 and 6 illustrate the experimental setup. It consists in a 4-kW, 220/380 V, 15/8.6 A, 50-Hz, 4 pole,  $\Delta$ -connected squirrel-cage induction motor. A separately excited dc generator feeding a variable resistor provided a mechanical load.

The induction motor has been initially tested, in absence of faults, in order to determine the stator currents corresponding to the supposed healthy motor (Fig. 7). Afterward, two kinds of experiments have been carried out. In the first one, stator voltages were unbalanced by adding a 0.2 p.u. resistance to one phase. The second one has concerned a single-phase effect corresponding to stator open phase. The stator currents corresponding to these faulty conditions are respectively shown by Figs. 8 and 9.

#### **5. FAULT DIAGNOSIS RESULTS**

Using the system depicted by Fig. 1, stator currents were measured (Figs. 7, 8 and 9) and their amplitudes derived.

These amplitudes were transferred into the corresponding discourse universe as inputs. The fuzzy logic inference engine evaluates the inputs using the knowledge base and then diagnoses the stator condition. In this final step, where fuzzy actions are reconverted to crisp ones, the “center of area” method has been adopted [5]. According to this method, first each affected output membership function is cut at the strength indicated by the previous max-rule, next the gravity center of the possible distribution is computed and it becomes the crisp output value.

For illustration, Figs. 10, 11, and 12 show fuzzy inference diagrams for different stator currents for which the induction motor stator condition is good, damaged, or seriously damaged. As it could be noticed, fuzzy rules are solicited, according to stator current amplitudes, leading to the determination of the motor condition.

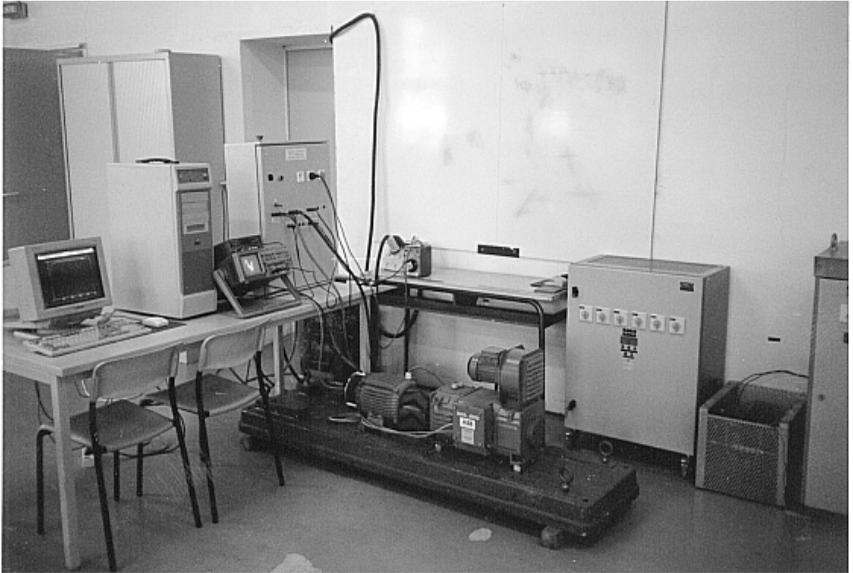


Fig. 5. View of the experimental setup.

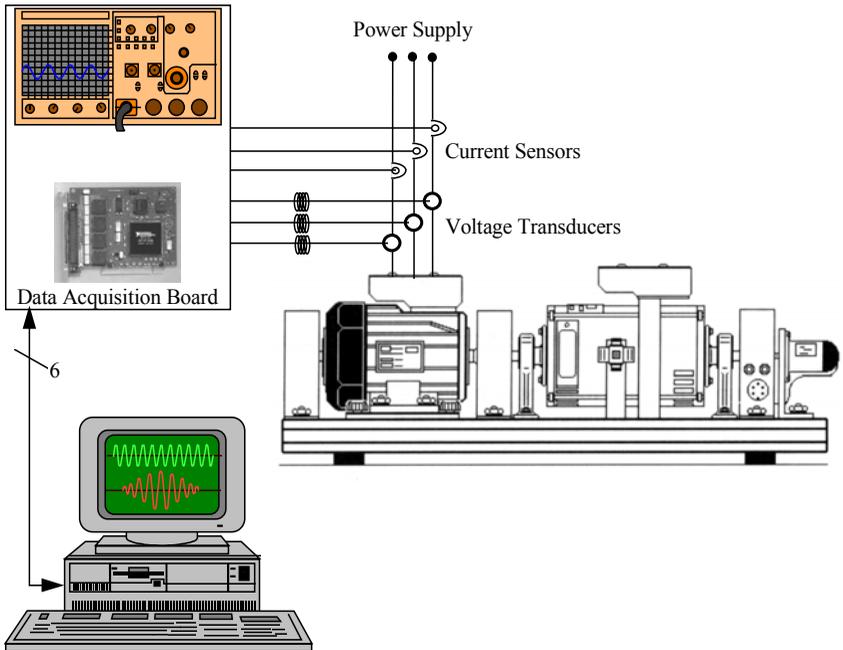
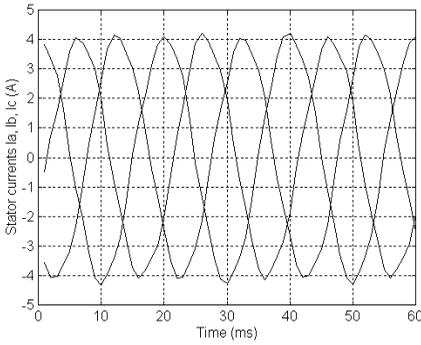
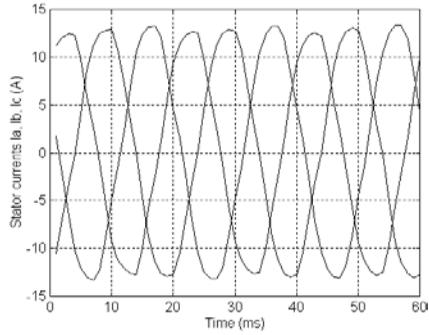


Fig. 6. Schematic view of the experimental set up.

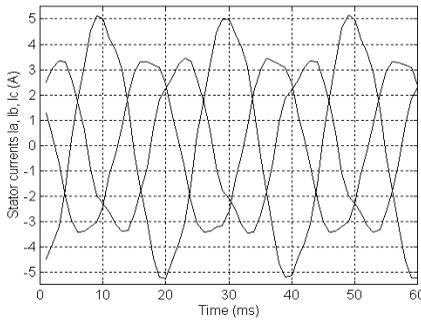


(a) Unloaded motor

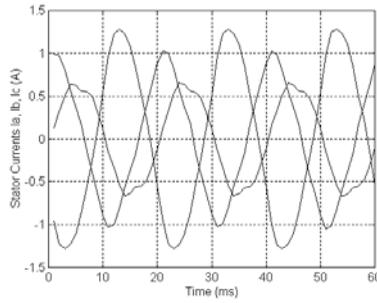


(b) Fully loaded motor.

Fig. 7. Induction motor healthy condition.

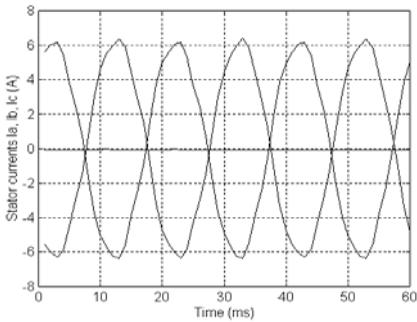


(a) Unloaded motor.

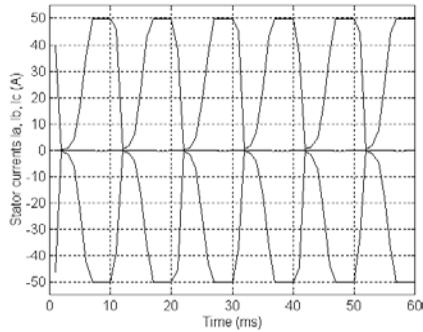


(b) Fully loaded motor.

Fig. 8. Stator currents for voltage unbalance.



(a) Unloaded motor.



(b) Fully loaded motor.

Fig. 9. Stator currents for open phase.

For Fig. 10, it is *rule (11)* that is solicited, in fact  $I_a = I_b = 5I_c = 5$  A are small “S”. The motor is in this case supposed healthy ( $CM = 0.05$ ). For Fig. 11, it is *rule (12)* that is solicited, in fact  $I_a = I_c = 5$  A are small “S”, and  $I_b = 15$  A is medium “M”. The motor is in this case damaged ( $CM = 0.5$ ). Finally, for Fig. 12, it is *rule (1)* that is solicited ( $I_a = 0$ ), or *rule (6)*, in  $I_c = 35$  A is big “B”. The motor is in this case seriously damaged ( $CM = 0.975$ ).

The performances of the proposed fuzzy logic approach, as shown in Table 1, are quite good. In fact, they indicate that it is capable of highly accurate diagnosis.

### 6. CONCLUSION

A method of using fuzzy logic to interpret current sensors signal of induction motor for its stator condition monitoring was presented. Correctly processing these current signals and inputting them to a fuzzy decision system achieved high diagnosis accuracy. There is most likely still room for improvement by using an intelligent means of optimization.

Table 1. Fuzzy logic fault diagnosis performance.

| Fault Detection                    | Diagnosis Accuracy |
|------------------------------------|--------------------|
| Good Conditions (Healthy Motor)    | 100%               |
| Bad Conditions (Voltage Unbalance) | 100%               |
| Severe Conditions (Open Phase)     | 94%                |

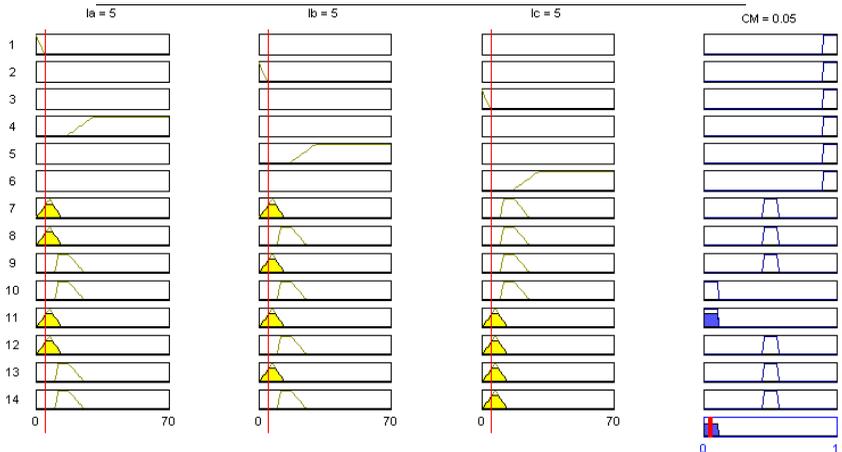


Fig. 10. Fuzzy inference diagram for a healthy motor.

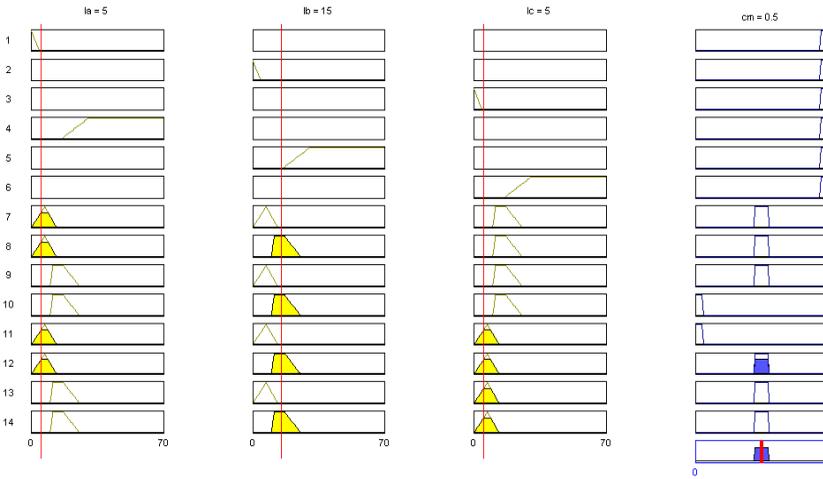


Fig. 11. Fuzzy inference diagram for a damaged motor.

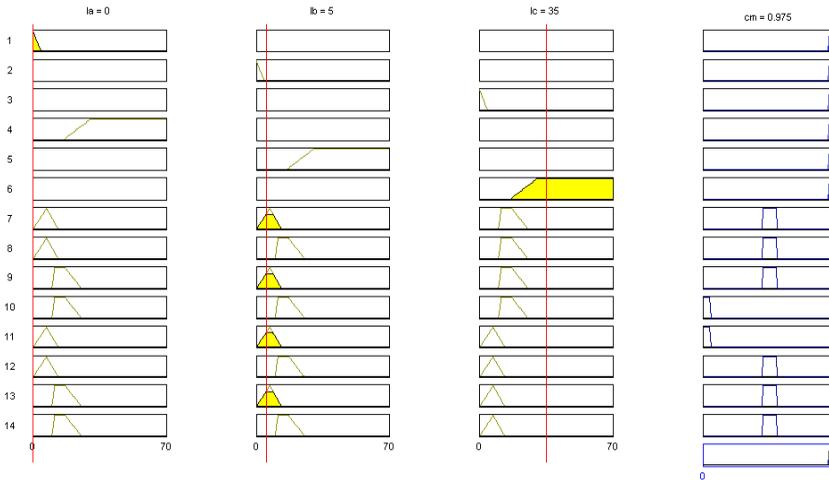


Fig. 12. Fuzzy inference diagram for a seriously damaged motor.

## APPENDIX

### Rated Parameters of the Induction Motor Under Test

|                        |          |                        |         |
|------------------------|----------|------------------------|---------|
| Power                  | 4kW      | Current ( $\Delta/Y$ ) | 15/8.6A |
| Frequency              | 50Hz     | Speed                  | 1440rpm |
| Voltage ( $\Delta/Y$ ) | 220/380V | Pole pair ( $p$ )      | 2       |

## REFERENCES

- [1] G.B. Kliman et al., Methods of motor current signature analysis, *Electric Machines & Power Systems*, vol. 20, n°5, September 1992, pp. 463-474.
- [2] G.B. Kliman et al., Sensorless online motor diagnostics, *IEEE Computer Applications in Power*, vol., 10, n°2, April 1997, pp. 39-43.
- [3] M.E.H. Benbouzid, A review of induction motors signature analysis as a medium for faults detection, *IEEE Trans. Industrial Electronics*, vol. 47, n°5, October 2000, pp. 984-993.
- [4] M.E.H. Benbouzid, Bibliography on induction motors faults detection and diagnosis, *IEEE Trans. Energy Conversion*, vol. 14, n°4, December 1999, pp. 1065-1074.
- [5] J.M. Mendel, Fuzzy logic systems for engineering: a tutorial, *Proceedings of the IEEE*, vol. 83, n°3, March 1995, pp. 345-377.
- [6] M.Y. Chow et al., *Motor Incipient Fault Detection Using Artificial Neural Network and Fuzzy Logic Technologies*, in Computer Aided Maintenance, Methodology and Practices. J. Lee, Ed.: Chapman Hall, 1996.
- [7] M.Y. Chow, *Methodologies of Using Neural Network and Fuzzy Logic Technologies for Motor Incipient Fault Detection*. Singapore: World Scientific Publishing Co. Pte. Ltd., 1997.
- [8] M.Y. Chow et al., *Intelligent Motor Fault Detection*, in Intelligent Techniques in Industry. L.C. Jain, Ed.: CRC Press, 1998.
- [9] H.J. Zimmermann, *Fuzzy Set Theory and Its Applications*. Kluwer Academic Publishers, 1991.
- [10] P.V. Goode et al., Neural/fuzzy systems for incipient fault detection in induction motors, *Proceedings of the 1993 International Conference of the IEEE Industrial Electronics Society*, Maui (USA).
- [11] E. Ritchie et al., Diagnosis of rotor faults in squirrel cage induction motors using a fuzzy logic approach,” *Proceedings of the 1994 International Conference on Electrical Machines*, Paris (France), vol. 2, pp. 348-352.
- [12] P.V. Goode et al., A hybrid fuzzy/neural system used to extract heuristic knowledge from a fault detection problem, *Proceedings of the 1994 IEEE World Congress on Computational intelligence*, Orlando (USA), vol. 3, pp. 1731-1736.
- [13] P.V. Goode et al., Using a neural/fuzzy system to extract knowledge of incipient fault in induction motors Part I - Methodology, *IEEE Trans. Industrial Electronics*, vol. 42, n°2, April 1995, pp., 131-138.
- [14] P.V. Goode et al., Using a neural/fuzzy system to extract knowledge of incipient fault in induction motors Part II - Application, *IEEE Trans. Industrial Electronics*, vol. 42, n°2, April 1995, pp. 139-146.

- [15] F. Filippetti et al., A fuzzy logic approach to on-line induction motor diagnostics based on stator current monitoring, *Proceedings of the 1995 IEEE International PowerTech Conference*, Stockholm (Sweden), vol. EMD, pp. 156-161.
- [16] N.M. Roehl et al., Fuzzy ART neural network approach for incipient fault detection and isolation in rotating machines, *Proceedings of the 1995 IEEE International Conference on Neural Networks*, vol. 1, pp. 538-542.
- [17] S. Altug et al., Comparative analysis of fuzzy inference systems implemented on neural structures, *Proceedings of the 1997 International Conference on Neural Networks*, Houston (USA), vol. 1, pp. 426-431.
- [18] S. Chun et al., A fuzzy expert system for vibration cause identification in rotating machines, *Proceedings of the 1997 IEEE International Conference on Fuzzy Systems*, vol. 1, pp. 555-560.
- [19] J. Boyce et al., Pump motor vibration analysis and fault detection using artificial neural/fuzzy system, *Proceedings of the 1997 International Conference on Maintenance and Reliability*, Knoxville (USA), vol. 2, pp. 60.01-60.15.
- [20] S. Caldara et al., A fuzzy diagnostic System: application to linear induction motor drives, *Proceedings of the 1997 IEEE Instrumentation and Measurement Technology Conference*, Ottawa (Canada), vol. 1, pp. 257-262.
- [21] M.Y. Chow et al., Set theoretic based neural-fuzzy motor fault detector, *Proceedings of the 1998 International Conference of the IEEE Industrial Electronics Society*, Aachen (Germany), vol. 4, pp. 1908-1913.
- [22] G. Goddu et al., Motor bearing fault diagnosis by a fundamental frequency amplitude based fuzzy decision system, *Proceedings of the 1998 International Conference of the IEEE Industrial Electronics Society*, Aachen (Germany), vol. 4, pp. 1961-1965.
- [23] T. Ross, *Fuzzy Logic with Engineering Applications*. New York: McGraw-Hill, 1995.
- [24] M.E.H. Benbouzid et al., Induction motor faults detection using advanced spectral analysis technique, *Proceedings of the 1998 International Conference on Electrical Machines*, Istanbul (Turkey), vol. 3, pp. 1849-1854.
- [25] M.E.H. Benbouzid et al., Induction motors faults detection and localization using stator current advanced signal processing techniques, *IEEE Trans. Power Electronics*, vol. 14, n°1, January 1999, pp. 14-22.
- [26] H.L. Poon, Verbal time series reports generation in condition monitoring, *Computers in Industry*, vol. 15, 1990, pp. 293-301.